Mass of Xenon in Vessel at Maximum Operating Pressure (absolute):

Assume we have either 100 or 200 kg. total Xe, and 85% of this comprises the active mass (volume of gas inside a cylinder inscribed within the QT/WLS assembly array), and 15% remains in plumbing and interstitial spaces:

$$M_{Xe~200} \coloneqq 170 kg \quad \text{@20bar}$$

or 
$$M_{Xe\ 100} := 85 kg$$

Maximum Operating pressures (absolute) for the 200/100 kg options:

$$P_{MOPa\ 200} = 20bar$$

$$P_{MOPa\ 100} := 10bar$$

Operating Temperature, physical constants:

$$T_{amb} := 293K$$

$$R := 8.314 \text{J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$$

$$R := 8.314 \text{J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$$
  $M_{a\_Xe} := 136 \text{gm} \cdot \text{mol}^{-1}$ 

Critical Pressure, temperature of Xenon:

$$P_{-} \mathbf{v}_{-} := 58.40 \text{bar}$$

$$P_{c Xe} := 58.40 \text{bar}$$
  $T_{c Xe} := 15.6 \text{K} + 273 \text{K}$   $T_{c Xe} = 288.6 \text{K}$ 

$$T_{c Xe} = 288.6 K$$

reduced pressure:

$$P_{r_{200}} := \frac{P_{MOPa_{200}}}{P_{c Xe}} \quad P_{r_{200}} = 0.3$$

$$P_{r\_200} := \frac{P_{MOPa\_200}}{P_{c Xe}} \quad P_{r\_200} = 0.342 \qquad \qquad P_{r\_100} := \frac{P_{MOPa\_100}}{P_{c Xe}} \quad P_{r\_100} = 0.171$$

reduced temperature

$$T_r := \frac{T_{amb}}{T_{c Xe}} \qquad T_r = 1.015$$

Compressibility Factors:

from chart for pure gasses shown below

$$Z_{Xe\ 20bar} := 0.87$$

$$Z_{Xe\ 10bar} := .96$$

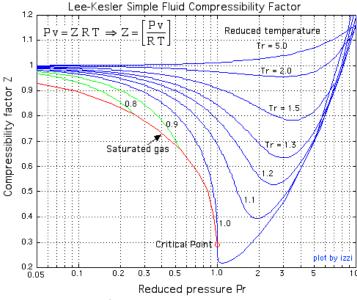


Fig. 6 Compressibility Factor, pure gasses

ref: A Generalized Thermodynamic Correlation based on Three-Parameter Corresponding States, B.I.Lee & M.G.Kesler, AIChE Journal, Volume 21, Issue 3, 1975, pp. 510-527' (secondary ref. from:http://www.ent.ohiou.edu/~thermo/

Number of moles:

$$n_{\text{Xe\_200}} := \frac{M_{\text{Xe\_200}}}{M_{a\_\text{Xe}}} \quad n_{\text{Xe\_200}} = 1.25 \times 10^3 \, \text{mol} \qquad n_{\text{Xe\_100}} := \frac{M_{\text{Xe\_100}}}{M_{a\_\text{Xe}}} \qquad n_{\text{Xe\_100}} = 625 \, \text{mol}$$

Volume required:

$$V_{Xe\_200} := \frac{{}^{n}Xe\_200^{\cdot}Z_{Xe\_20bar} \cdot R \cdot T_{amb}}{{}^{p}MOPa\_200} \qquad V_{Xe\_200} = 1.307 \, \text{m}^{3}$$

$$V_{Xe\_100} := \frac{{}^{n}Xe\_100^{\cdot}Z_{Xe\_10bar} \cdot R \cdot T_{amb}}{{}^{p}MOPa\_100} \qquad V_{Xe\_100} = 1.442 \, \text{m}^{3}$$

Since chamber will be designed for 20 bar, we can tolerate slightly higher than 10 bar pressure at 100 kg, so we design for the smaller volume:

$$n_{Xe} := n_{Xe\_200}$$
  $V_{Xe} := V_{Xe\_200}$   $P_{MOPa} := P_{MOPa\_200}$ 

molar, mass, volumetric density:

$$\begin{split} \rho_{mol} &\coloneqq \frac{^{n}Xe}{^{V}Xe} \quad \rho_{mol} = 0.956 \frac{mol}{L} \\ \rho_{Xe} &\coloneqq \rho_{mol} \cdot M_{a\_Xe} \quad \rho_{Xe} = 0.13 \frac{gm}{cm^{3}} \\ v_{Xe} &\coloneqq \rho_{Xe}^{-1} \quad v_{Xe} = 7.688 \frac{cm^{3}}{gm} \end{split}$$

We desire active length to be = 1.25x active diameter. then:

$$\begin{array}{ll} \text{Active volume radius:} & r_{Xe} \coloneqq \sqrt[3]{\frac{V_{Xe}}{2.5\pi}} & r_{Xe} = 0.550\,\text{m} \\ \text{and} & l_{Xe} \coloneqq 2.5r_{Xe} & l_{Xe} = 1.375\,\text{m} \end{array}$$

Quartz Tube (QT) length:

items using up at length (full length at is needed):

shield: 
$$l_{shld} := 20cm$$

EL grid frameset: 
$$l_{EL} := 3cm$$

cathode plane: 
$$l_{cath} := 3cm$$

QT length:

$$l_{qt} := l_{Xe} + (l_{shld} + l_{SiPMT} + l_{EL} + l_{cath})$$
  $l_{qt} = 1.645 \,\text{m}$ 

Maximum available quartz tube length is over 2m so we are OK.

QT tube outer radius:

$$r_{qt} := 21 mm$$

QT/WLS sys. nom radius (at QT axis)

$$R_{wls} := r_{Xe} + r_{qt}$$
  $R_{wls} = 0.571 \,\mathrm{m}$ 

QT dimensional tolerances

bow: OD (+/-) ovality  $\begin{aligned} \text{tol}_{bow} &\coloneqq 1.5 \frac{\text{mm}}{\text{m}} \cdot l_{qt} \\ \text{tol}_{bow} &= 2.468 \, \text{mm} \end{aligned} \end{aligned} \quad \begin{aligned} \text{tol}_{OD} &\coloneqq 1 \text{mm} \\ \text{tol}_{OV} &\coloneqq 0.5 \text{tol}_{OD} \\ \text{tol}_{OV} &= 0.5 \, \text{mm} \end{aligned}$ 

total tolerance:

 $N_{at} := 75$ 

Angle of QT spacing  $\theta_{qt} := \frac{360 deg}{N_{qt}} \qquad \theta_{qt} = 4.8 \, deg$ 

Tangential QT spacing (nominal):

 $s_{qt} \coloneqq R_{wls} \cdot \sin(\theta_{qt}) - 2r_{qt} \qquad \qquad s_{qt} = 5.782 \, \text{mm} \quad \text{check that} \quad s_{qt} > \text{tol}_{tot} \qquad \text{tol}_{tot} = 3.968 \, \text{mmOK}$ 

Xenon vessel inner radius, min.:

 $R_{i \text{ Xev min}} := r_{Xe} + 2r_{qt} + tol_{tot} + 1mm$   $R_{i \text{ Xev min}} = 0.597 \text{ m}$ 

Set Xenon vessel inner radius to:

$$R_{i Xev} := 0.6m$$

Note that this assumes there is no cylindrical reflector and gas distribution annulus outside the QT/WLS array and Xenon gas distribution pipes (PTFE) are located in the interstitial spaces behind the QTs.

Xenon Vessel wall thickness

 $t_{XeV} \coloneqq 1cm$  Note, this is likely a practical minimum which allows sealing and fastener attachment at flange; wall thickness can be thinner elsewhere (see below), and some outward extension past this at the cathode may be permissible.

Buffer gas annulus thickness, at main service flange

 $t_{bg} \coloneqq 2cm$  Though this annulus is tapered, the EL "cathode" grid HV will be near the flange and will have a substantial voltage (?30 kV). Also, the HV cable feeding the EL cathode grid will enter in through this annulus and has a finite width, of perhaps 7mm

Pressure Vessel inner radius:

$$R_{i_pv} := R_{i_xev} + t_{Xev} + t_{bg}$$
  $R_{i_pv} = 0.63 \text{ m}$ 

Vessel wall thicknesses

Pressure vessel

maximum allowable material stresses, from ASME 2009 Pressure Vessel code, sec. II part D, table 1B:

Grade 1 Titanium  $S_{\text{max Ti g1}} := 10000 \text{psi}$ 

Grade 2 Titanium  $S_{\text{max Ti g2}} := 14300 \text{psi}$ 

(all annealed) Grade 9 Titanium (3AI-2.5V)  $S_{\text{max}}$   $T_{i}$   $g_{9} := 25700 \text{psi}$ 

Grade 10200-O25 Copper (OF)  $S_{max}$  C10200 := 6700psi

Maximum Operating Pressure (MOP), gauge:

$$MOP_{pv} := (P_{MOPa} - 1bar)$$
  $MOP_{pv} = 19 bar$ 

Maximum allowable pressure, gauge (from LBNL Pressure Safety Manual, PUB3000) at a minimum, 10% over max operating pressure:

$$MAWP_{pv} := 1.1MOP_{pv}$$
  $MAWP_{pv} = 20.9 bar$ 

then, for inner radius:  $R_{i pv} = 0.63 \text{ m}$ 

for both xenon and pressure vessels, use ASME code formula (sec VIII, UG-27, eq(1) for min vessel wall  $E_w \coloneqq 1 \quad \begin{array}{l} \text{maximum weld efficiency: use fusion (E-beam} \\ \text{or diffusion) welding and radiograph welds} \end{array}$ thickness:

minimum wall thickness, grade 2 Titanium:

$$E_{\rm w} := 1$$
 or diffusion) welding and radiograph welds

$$t_{pv\_min\_g2} := \frac{MAWP_{pv} \cdot R_{i\_pv}}{S_{max\_Ti\_g2} \cdot E_w - 0.6 \cdot MAWP_{pv}}$$
  $t_{pv\_min\_g2} = 1.371 \text{ cm}$ 

minimum wall thickness, grade 9 Ti (3AI-2.5V)

$$t_{pv\_min\_g9} := \frac{MAWP_{pv} \cdot R_{i\_pv}}{S_{max\_Ti\_g9} \cdot E_w - 0.6 \cdot MAWP_{pv}} \qquad t_{pv\_min\_g9} = 0.759 \text{ cm}$$

minimum wall thickness, Copper, OF grade, annealed

$$t_{pv\_min\_Cu} := \frac{MAWP_{pv} \cdot R_{i\_pv}}{S_{max\_C10200} \cdot E_w - 0.6 \cdot MAWP_{pv}} \qquad t_{pv\_min\_Cu} = 2.971 \, cm$$

Note that this is nominal wall thickness, not near flanges; main service flange thickness will be determined by bending moments from fastener loads. Also at cathode end, radius is larger and will require a proportional thickness increase.

Xenon inner vessel minimum wall thickness:

use max. stress in PMMA = 0.1Sy

$$S_{y\_PMMA} := 78MPa$$
  $S_{y\_PMMA} = 1.131 \times 10^4 \text{ psi}$ 

$$S_{\text{max\_PMMA}} := 0.1S_{\text{y\_PMMA}}$$
  $S_{\text{max\_PMMA}} = 7.8 \times 10^6 \text{ Pa}$ 

Assume maximum differential pressure:  $dP_{Xe} := 0.1bar$ 

 $t_{\text{Xe\_min}} := \frac{dP_{\text{Xe}} \cdot R_{i\_\text{Xev}}}{0.1S_{v\_PMMA} - 0.6dP_{\text{Xe}}}$   $t_{\text{Xe\_min}} = 0.078 \text{ cm}$ then, minimum thickness: